STATISTICS AND PROBABILITY

Department of Statistics and Probability College of Natural Science

200 Statistical Methods

Fall, Spring, Summer. 3(4-0) P: (MTH 103 or MTH 110 or MTH 116 or MTH 124 or MTH 132 or LB 118) or designated score on Mathematics Placement test Not open to students with credit in STT 201 or STT 421.

STT

Data analysis, probability models, random variables, estimation, tests of hypotheses, confidence intervals, and simple linear regression.

201 Statistical Methods

Fall, Spring, Summer. 4(3-2) P: (MTH 103 or MTH 110 or MTH 116 or MTH 124 or MTH 132 or LB 118) or designated score on Mathematics Placement test Not open to students with credit in STT 200 or STT 421.

Probability and statistics with computer applications. Data analysis, probability models, random variables, tests of hypotheses, confidence intervals, simple linear regression. Weekly lab using statistical software.

224 Introduction to Probability and Statistics for Ecologists

Spring. 3(2-2) Interdepartmental with Fisheries and Wildlife. Administered by Statistics and Probability. P: MTH 103 or MTH 116 or (MTH 124 or concurrently) or (MTH 132 or concurrently) or (MTH 152H or concurrently) or (LB 118 or concurrently) RB: BS 162 or BS 182H or LB 144 SA: FW 324 Not open to students with credit in STT 231.

Probability and statistics with computer applications for the analysis, interpretation and presentation of ecological data. Data analysis, probability models, random variables, estimation, confidence intervals, test of hypotheses, and simple linear regression with applications to ecology.

231 Statistics for Scientists

Fall, Spring, Summer. 3(3-0) P: MTH 124 or MTH 132 or MTH 152H or LB 118 R: Open to students in the College of Natural Science and open to students in the Lyman Briggs College. SA: STT 331

Calculus-based course in probability and statistics. Probability models, and random variables. Estimation, confidence intervals, tests of hypotheses, and simple linear regression with applications in sciences.

250 Statistics and Probability for K-8 Teachers

Spring. 4(4-0) P: MTH 103 R: Open to undergraduate students in the College of Education or approval of department.

Data collection and analysis. Statistics, probability models. Decision-making in the presence of variability. Computer software relevant for teaching practice.

290 Topics in Statistics and Probability

Fall, Spring, Summer. 1 to 3 credits. RB: MTH 103 R: Approval of department. Individualized study of selected topics. 301 Computational Methods for Data Science Fall. 3(3-0) P: (MTH 132 or LB 118 or MTH 152H) and (STT 200 or STT 201 or STT 231 or STT 315 or STT 421 or STT 441)

Obtaining and managing data using statistical software. Data visualization and graphics. Special challenges in working with high-dimensional data.

315 Introduction to Probability and Statistics for Business

Fall, Spring, Summer. 3(4-0) P: MTH 124 or MTH 132 or MTH 152H or LB 118

A first course in probability and statistics primarily for business majors. Data analysis, probability models, random variables, confidence intervals, and tests of hypotheses with business applications.

317 Quantitative Business Research Methods

Fall, Spring, Summer. 3(3-0) Interdepartmental with Marketing. Administered by Marketing. P: STT 315 R: Open to juniors or seniors in the Eli Broad College of Business and The Eli Broad Graduate School of Management and not open to undergraduate students in the School of Hospitality Business and open to juniors or seniors in the Applied Engineering Sciences major. SA: MSC 317

Application of statistical techniques, including forecasting, to business decision making. Includes applications of linear regression and correlation, analysis of variance, selected non-parametric tests, time series, and index numbers.

351 Probability and Statistics for Engineering Fall, Spring, Summer. 3(3-0) P: MTH 234 or MTH 254H or LB 220 Not open to students with credit in STT 430.

Probability models and random variables. Estimation, confidence intervals, tests of hypotheses, simple linear regression. Applications to engineering.

421 Statistics I

Fall, Spring, Summer. 3(3-0) P: MTH 103 or MTH 110 or MTH 116 Not open to students with credit in STT 200 or STT 201.

Basic probability, random variables, and common distributions. Estimation and tests for one-, two-, and paired sample problems. Introduction to simple linear regression and correlation, one-way ANOVA.

422 Statistics II

Fall, Spring, Summer. 3(3-0) P: STT 421 Not open to students with credit in STT 464.

Goodness of fit and other non-parametric methods. Linear models including multiple regression and ANOVA for simple experimental designs.

430 Introduction to Probability and Statistics

Fall, Spring, Summer. 3(3-0) P: (MTH 234 or concurrently) or (MTH 254H or concurrently) or (LB 220 or concurrently) Not open to students with credit in STT 351.

Calculus-based probability and statistics with applications. Discrete and continuous random variables and their expectations. Point and interval estimation, tests of hypotheses, and simple linear regression.

441 Probability and Statistics I: Probability

Fall, Spring, Summer. 3(3-0) P: MTH 234 or MTH 254H or LB 220 or approval of college Probability models and basic statistics at an interme-

Probability models and basic statistics at an intermediate mathematical level. Discrete, continuous, univariate, and multivariate distributions. Random variables. Normal approximation. Sampling distributions, parameter estimation, and elementary tests of hypotheses.

442 Probability and Statistics II: Statistics

Spring. 3(3-0) P: STT 441 and (MTH 309 or MTH 314 or MTH 317H or MTH 415)

Estimation, testing hypotheses and simple and multiple regression analysis. Time series: ARMA (Auto Regressive Moving Average) and ARIMA (Auto Regressive Integrated Moving Average) models, data analysis and forecasting.

455 Actuarial Models I

Fall. 3(3-0) Interdepartmental with Mathematics. Administered by Statistics and Probability. P: STT 441 and MTH 360

Stochastic models used in insurance. Survival distributions, life insurance, life annuities, benefit premiums, benefit reserves, and analysis of benefit reserves.

456 Actuarial Models II

Spring. 3(3-0) Interdepartmental with Mathematics. Administered by Statistics and Probability. P: STT 455

Continuation of STT 455. Benefit reserves. Multiple life functions. Multiple decrement models and their applications. Elements of stochastic processes for actuaries including Markov chains and Poisson processes

458 Financial Mathematics for Actuaries II

Fall. 3(3-0) Interdepartmental with Mathematics. Administered by Mathematics. P: MTH 361 and STT 441 RB: MTH 235 or MTH 340 or MTH 347H

Evaluate and construct interest rate models. Rational valuation of derivative securities using put-call parity and calculation of European and American options. Risk management techniques using the method of delta-hedging.

459 Construction and Evaluation of Actuarial Models

Spring. 3(3-0) Interdepartmental with Mathematics. Administered by Statistics and Probability. P: STT 442

Severity, frequency, and aggregate models. Construction of empirical models. Parametric statistical methods. Credibility analysis. Simulation methods.

461 Computations in Probability and Statistics

Spring. 3(3-0) P: (STT 441 and CSE 231) and (MTH 309 or MTH 314 or MTH 317H or MTH 415)

Computer algorithms for evaluation, simulation and visualization. Sampling and prescribed distributions. Robustness and error analysis of procedures used by statistical packages. Graphics for data display, computation of probabilities and percentiles.

464 Statistics for Biologists

Fall. 3(3-0) Interdepartmental with Animal Science and Crop and Soil Sciences. Administered by Statistics and Probability. P: MTH 103 or MTH 110 or MTH 116 RB: STT 421

Biological random variables. Estimation of population parameters. Testing hypotheses. Linear correlation and regression. Analyses of counted and measured data to compare several biological groups including contingency tables and analysis of variance.

465 Bayesian Statistical Methods

Fall. 3(3-0) A student may earn a maximum of 0 credits none Interdepartmental with Epidemiology. Administered by Statistics and Probability. P: STT 442

Probability, P: STT 442
Probability, belief, and exchangeability. Objective, subjective, and empirical Bayes approaches. Applications to one-parameter models, linear regression models, and multivariate normal models. Hierarchical modeling. Computational methods.

481 Capstone in Statistics (W)

Spring. 3(3-0) P: (STT 442 or approval of department) and completion of Tier I writing requirement R: Open to seniors in the Department of Statistics and Probability or approval of department.

Selected readings and projects illustrating special problems encountered by statisticians in their roles as consultants, educators, researchers and analysts.

490 Directed Study of Statistical Problems

Fall, Spring, Summer. 1 to 3 credits. A student may earn a maximum of 9 credits in all enrollments for this course. R: Open to seniors in the Department of Statistics and Probability. Approval of department.

Individualized study of selected topics.

801 Design of Experiments

Fall of even years. 3(3-0) RB: STT 422 or STT 442 or STT 471

Blocking and randomization. Split-plot, latin square and factorial designs. Fractional factorial designs, aliasing and confounding of effects. Mixture and central composite designs and response surface exploration. Clinical trials.

802 Statistical Computation

Fall of even years. 3(3-0) RB: (STT 442 and MTH 309) or (mathematical statistics and linear algebra)

Computational techniques commonly used in Statistics. Matrix decompositions. Least squares and Least Absolute Deviations. Solution of nonlinear equations. Optimization techniques including the EM algorithm and constrained optimization. Numerical integration. Generation of random numbers and stochastic simulation. Implementation in statistical soft-

805 Statistical Modeling for Business Analytics

Summer. 3(3-0) RB: STT 442 R: Open to master's students in the Business Analytics Major

Low dimensional data visualization. Simple linear regression. Regression diagnostics. Analysis of variance. Multiple linear regression. Regression model building. Variable selection. Categorical data. Logistic regression. Proportional odds model. Introduction to time series.

808 Biostatistics I

Fall. 3(3-0) Interdepartmental with Epidemiology. Administered by Epidemiology. RB: College-level algebra. R: Open to master's students or doctoral students in the Epidemiology major or approval of department. SA: STT 425

Applications of probability and statistics in the applied health sciences. Probability distributions, estimation and tests for one-, two-, and paired samples, linear regression, correlation, and ANOVA. Use of statistical software. Critical appraisal of statistical methods in the biomedical literature.

809 Biostatistics II

Spring. 3(3-0) Interdepartmental with Epidemiology. Administered by Epidemiology. P: EPI 808 RB: MTH 103 or MTH 110 or MTH 116 R: Open to master's students or doctoral students in the Epidemiology major or approval of department. SA: STT 426

Analysis of categorical data in epidemiologic studies. Contingency tables and logistic regression.

814 Advanced Statistics for Biologists

Spring. 4(3-2) Interdepartmental with Animal Science and Crop and Soil Sciences. Administered by Statistics and Probability. RB: STT 464

Concepts of reducing experimental error for biological and agricultural research. Covariance, randomized block designs, latin squares, split plots, repeated-measures designs, regression applications, and response surface designs. Analyses using statistical software.

820A Econometrics IA

Fall. 3(3-0) Interdepartmental with Economics. Administered by Economics. R: Open only to doctoral students in the Economics major or the Department of Agricultural Economics or the Business Administration major or approval of department.

Statistical tools for econometrics. Applications of statistical tools, including probability distributions, estimation, hypothesis testing, and maximum likelihood to econometric problems.

821A Cross Section and Panel Data Econometrics I

Fall. 3(3-0) Interdepartmental with Agricultural Economics and Economics and Finance. Administered by Economics. P: EC 820B SA: EC 821

Analyses of systems of equations, panel data models, instrumental variables and generalized method of moments, M-estimation, quantile regression, maximum likelihood estimation, binary and multinomial response models, Tobit and two-part models, and other selected topics.

821B Cross Section and Panel Data Econometrics II

Spring. 3(3-0) Interdepartmental with Agricultural, Food, and Resource Economics and Economics and Finance. Administered by Economics. P: EC 821A

Analyses of quasi-maximum likelihood estimation, count data models, fractional response models, duration models, sample selection and attrition, stratified sampling, estimating treatment effects, stochastic frontier models, and other advanced topics.

822A Time Series Econometrics I

Fall. 3(3-0) Interdepartmental with Agricultural Economics and Economics and Finance. Administered by Economics. P: EC 820B SA: EC 822

Analyses of time series regression, stationary time series analysis, ARMA models, Wold decomposition, spectral analysis, vector autoregressions, generalized method of moments, functional central limit theorem, nonstationary time series, unit root processes, cointegration, and other advanced topics.

822B Time Series Econometrics II

Spring. 3(3-0) Interdepartmental with Agricultural Economics and Economics and Finance. Administered by Economics. P: EC 822A

Analyses of multivariate time series, time series volatility models, long memory, nonlinear time series models, and other advanced topics.

825 Sample Surveys

Fall. 3(3-0) RB: STT 422 or STT 442 or STT 862

Application of statistical sampling theory to survey designs. Simple random, stratified, and systematic samples. Sub-sampling, double sampling. Ratio and regression estimators.

843 Multivariate Analysis

Spring of even years. 3(3-0) RB: STT 442 or STT 862 Not open to students with credit in FW 850.

Multivariate normal distribution, tests of hypotheses on means, multivariate analysis of variance. Discriminant analysis. Principal components. Factor analysis. Analysis of frequency data.

844 Time Series Analysis

Spring of odd years. 3(3-0) RB: STT 442 or STT 862

Stationary time series. Autocorrelation and spectra. ARMA and ARIMA processes: estimation and forecasting. Seasonal ARIMA models. Identification and diagnostic techniques. Multivariate time series. Time series software.

847 Analysis of Survival Data

Spring of odd years. 3(3-0) Interdepartmental with Epidemiology. Administered by Statistics and Probability. RB: STT 422 or STT 442 or STT 862

Analysis of lifetime data. Estimation of survival functions for parametric and nonparametric models. Censored data. The Cox proportional hazards model. Accelerated failure time models. Frailty models. Use of statistical software packages.

849 Applied Bayesian Inference using Monte Carlo Methods for Quantitative Biologists

Fall of even years. 3(2-2) Interdepartmental with Animal Science and Fisheries and Wildlife. Administered by Fisheries and Wildlife. RB: (STT 814 and IBIO 851) or equivalent courses. R: Not open to undergraduate students.

Applications of Bayesian inference using software in quantitative biology and genetics. Hierarchical and non-hierarchical models. Model checking, model selection and model comparison. Markov chain Monte Carlo methods

850 Applied Multivariate Statistical Methods

Spring of even years. 4(3-2) Interdepartmental with Fisheries and Wildlife. Administered by Fisheries and Wildlife. RB: (STT 422 or concurrently) and MTH 314 SA: FOR 976

Application of multivariate methods to research problems. Hotelling's T-test, profile analysis, discriminant analysis, canonical correlation, principal components, principal coordinates, correspondence analysis, and cluster analysis.

855 Statistical Genetics

Fall of odd years. 3(3-0) RB: STT 442 or STT 862

Probabilistic and statistical methods for genetic linkage and association studies. Quantitative trait locus mapping.

861 Theory of Probability and Statistics I

Fall. 3(3-0) RB: MTH 234 and MTH 309
Probability models, random variables and vectors.
Special distributions including exponential family.
Expected values, covariance matrices, moment generating functions. Convergence in probability and distribution. Weak Law of Large Numbers and Lyapunov Central Limit Theorem.

862 Theory of Probability and Statistics II Spring. 3(3-0) P: STT 861

Statistical inference: sufficiency, estimation, confidence intervals and testing of hypotheses. One and two sample nonparametric tests. Linear models and Gauss-Markov Theorem.

863 Statistical Methods I

Fall. 3(3-0) RB: (STT 442 or STT 862) and MTH 415 SA: STT 841

Introduction to the general theory of linear models. Application of regression models. Interval estimation, prediction and hypothesis testing. Contrasts; model diagnostics; model selection. LASSO type and high dimensional variable selection. Introduction to Linear mixed effect models.

864 Statistical Methods II

Spring. 3(3-0) P: STT 863 Generalized linear models(GLMs). Deviance and residual analysis in GLMs. Analysis of two-way and three-way contingency tables. Logistic regression. Log-linear models. Multicategorical response models. Poisson regression. Introduction to generalized estimating equations. Introduction to longitudinal data. Bayesian analysis using WinBUGS.

866 **Spatial Data Analysis**

Fall. 4(3-2) Interdepartmental with Geography. Administered by Geography. RB: (GEO 363 or STT 421 or STT 430) or equivalent quantitative methods courses. SA: GEO 466

Theory and techniques for statistical analysis of point patterns, spatially continuous data, and data in spatial zones.

867

Linear Model MethodologyFall. 3(3-0) P: STT 862 R: Open to doctoral students in the Department of Statistics and Probability or approval of department.

Properties of the multivariate normal distribution, Cochran's Theorem, simple and multiple linear regression models, Gauss-Markov Theorem, best linear unbiased prediction, one- and two-way ANOVA models, sums of squares, diagnostics and model selection, contingency tables and multinomial models, generalized linear models, logistic regression.

868 Mixed Models: Theory, Methods and **Applications**

Spring. 3(3-0) P: STT 867 R: Open to doctoral students in the Statistics major or approval of department.

Maximum likelihood estimation and other estimation methods for linear mixed models. Statistical properties of LME models. Prediction under LME models. Generalized linear mixed models. Quasi-likelihood estimation, generalized estimating equations for GLMM. Nonlinear mixed models. Diagnostics and influence analysis. Bayesian development in mixed linear models. Application of mixed models.

872

Statistical Inference I Spring. 3(3-0) P: STT 862 and STT 881 R: Open to doctoral students in the Statistics major or approval of department.

Statistical distributions, decision-theoretic formulation of estimation and testing of hypotheses, sufficiency, Rao-Blackwellization, admissibility, Bayes and minimax estimation, maximum likelihood estimation, inference based on order statistics, Neyman-Pearson Lemma and applications, multiple testing

Statistical Learning and Data Mining 873

Fall of odd years. 3(3-0) P: STT 868 and STT 872 R: Open to doctoral students in the Statistics major or approval of department.

Statistical methods focusing on machine learning and data mining, modern regression and classification techniques, support vector machines, boosting, kernel methods and ensemble methods, clustering dimension reduction, manifold learning, and selected topics.

874 Introduction to Bayesian Analysis

Fall of even years. 3(3-0) P: STT 868 and STT 872 R: Open to doctoral students in the Statistics major or approval of department.

Bayesian methods including empirical Bayes, hierarchical Bayes and nonparametric Bayes, computational methods for Bayesian inference including the Gibbs Sampler and Metropolis-Hastings method, and applications.

Theory of Probability I 881

Fall. 3(3-0) P: STT 861 and MTH 421 R: Open to doctoral students in the Statistics major or approval of department.

Measures and their extensions, integration. Lp spaces and Inequalities. Lebesgue decomposition, the Radon-Nikodym theorem. Product measures, Fubini's theorem. Kolmogorov consistency theorem. Independence, Kolmogorov's zero-one law, the Borel-Cantelli lemma. Law of large numbers. Central limit theorems, characteristic functions, the Lindeberg-Feller theorem, asymptotic normality of sample median. Poisson convergence. Conditional expectations.

Theory of Probability II

Spring. 3(3-0) P: STT 881 R: Open to doctoral students in the Statistics major or approval of department.

Random walks, transcience and recurrence. Martingales, martingale convergence theorem, Doob's inequality, optional stopping theorem. Stationary processes and Ergodic theorem. Brownian motion. Kolmogorov's continuity theorem, strong Markov property, the reflection principle, martingales related to Brownian motion. Weak convergence in C([0,1]) and D([0,1]), Donsker's invariance principle, empirical processes.

886 **Stochastic Processes and Applications** Fall. 3(3-0) RB: STT 441 or STT 861

Markov chains and their applications in both discrete and continuous time, including classification of states, recurrence, limiting probabilities. Queuing theory, Poisson process and renewal theory.

Stochastic Models in Finance

Spring of even years. 3(3-0) RB: STT 441 or STT 861 SA: STT 887

Stochastic models used in pricing financial derivatives. Discrete-time models. Brownian motion. Sto-chastic integrals and Ito's formula. Basic Black-Scholes model. Risk neutral distribution. European and American options. Exotic options. Interest rate market, futures, and interest rate options.

Statistical Problems

Fall, Spring, Summer. 1 to 3 credits. A student may earn a maximum of 24 credits in all enrollments for this course. R: Approval of department.

Individualized study on selected problems

Master's Thesis Research 899

Fall, Spring, Summer. 1 to 6 credits. A student may earn a maximum of 36 credits in all enrollments for this course. R: Approval of department.

Master's thesis research.

914 **Advanced Organizational Research** Methods

Spring. 3(3-0) Interdepartmental with Management. Administered by Management. P: MGT 906

Methods for empirically testing scientific theories in organizational contexts.

920 Advanced Methods in Epidemiology and **Applied Statistics**

Spring. 3(3-0) Interdepartmental with Epidemiology. Administered by Epidemiology. P: (EPI 826B or concurrently) or EPI 826 or approval of department R: Open to graduate students in the Department of Epidemiology and Biostatistics or approval of department.

Pattern recognition and cluster analysis, longitudinal data analysis, path analysis, repeated measures and time-series analysis.

Statistical Inference II 951

Spring of odd years. 3(3-0) P: STT 872 and STT 882 R: Open to doctoral students in the Statistics major or approval of department.

Decision theoretic estimation: Minimaxity, admissibil-

ity, shrinkage estimators, James-Stein estimators. Advanced estimation theory, maximal invariant tests, multiple testing, FDR, and related methods. Permutation and rank tests, unbiasedness and invariance, Hunt Stein theorem.

953 **Asymptotic Theory**

Spring of even years. 3(3-0) P: STT 872 and STT 882 R: Open to doctoral students in the Statistics major or approval of department.

Locally asymptotic normal models, empirical likelihood, U-statistics, Asymptotically efficient and adaptive procedures

961 Weak Convergence and Asymptotic

Fall of odd years. 3(3-0) P: STT 872 and STT 882 R: Open to doctoral students in the Statistics major or approval of department.

Maximal inequalities, covering numbers, symmetrization technique, Glivenko-Cantelli Theorems, Donsker Theorems and some results for Gaussian processes, Vapnik-Chervonenkis classes of sets and functions, applications to M-estimators, bootstrap, delta-method

Fractional Processes and Power Laws

Spring of even years. 3(3-0) P: STT 872 and STT 882 R: Open to doctoral students in the Statistics major or approval of department.

Self-similar processes. Fractional Brownian motion, fractional stable motions. Fractional calculus, Laplace and Fourier transforms, semigroups and generators. Continuous time random walks. Connections between long range dependence, heavy tails, and fractional calculus. Inference for processes with long range dependence and heavy tails, including fractional ARIMA models, ARCH/GARCH models, and random difference equations.

Stochastic Analysis

Spring of even years. 3(3-0) RB: STT 882 Stochastic integrals and semi-martingales, Ito formula, stochastic differential equations. Applications.

990 **Problems in Statistics and Probability**

Fall, Spring, Summer. 1 to 3 credits. A student may earn a maximum of 6 credits in all enrollments for this course. RB: STT 872 R: Approval of department.

Individual study on an advanced topic in statistics or probability.

Advanced Topics in Probability

Fall, Spring, Summer. 3(3-0) A student may earn a maximum of 15 credits in all enrollments for this course. RB: STT 882 R: Approval of department.

Current topics in probability.

Statistics and Probability—STT

997

Advanced Topics in Statistics Fall, Spring, Summer. 3(3-0) A student may earn a maximum of 15 credits in all enrollments for this course. RB: STT 872 R: Ap-

proval of department.

Topics selected from non- and semi parametric statistics, multivariate analysis, time series analysis, Bayesian statistics, regression and kernel estimation, and other topics in advanced statistics.

Doctoral Dissertation Research
Fall, Spring, Summer. 1 to 24 credits. A student may earn a maximum of 36 credits in all enrollments for this course. R: Approval of department.

Doctoral dissertation research.