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# A Network Theory-Based Approach To Pricing Cyber Risk

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# Agenda

## Introduction

### Constructing a Model

- Network Theory – The ABC's
- Organization Network Infrastructure
- Determining Spread of Attacks
- Impact of Corporate Social Networks
- Risk Scenarios

### Using the Model for Pricing

- Data Vulnerability and Value
- Business Interruption
- Insuring Specific Nodes and Sub-Networks
- Other Uses

### Takeaways and Conclusions

### Q&A





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# Introduction

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# Cyber Risk – What, How and Why?

## What?

Damaging a company's operations and/or reputation through its data and/or its IT infrastructure

Broad categories:

- Data breaches
- Business interruption
- System hijacking

## How?

Social Engineering (like Phishing)

Ransomware

Password Theft

Malware (like Trojan viruses)

Eavesdropping

DDOS

SQL Injections

Man-In-The-Middle

Accidental Node Failure

## Why?

**Money** – Kaseya 2021  
(Amateurs, Criminals, Many)

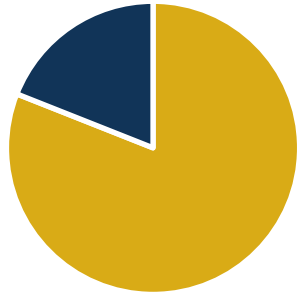
**Espionage** – Sony 2014  
(Competitors, Governments)

**Political/Personal**  
(Hacktivists, ex-employees)

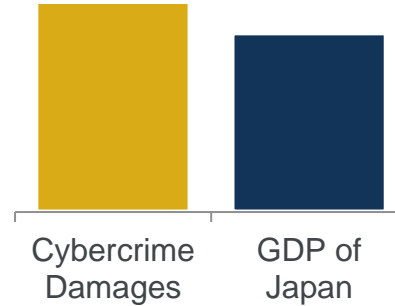
**Accidental** – AWS 2017  
(carelessness, mistakes)



# Cyber Risk and the Insurance Market Today



2021 Munich Re  
Global Cyber Risk  
survey: only 19%  
C-level respondents  
feel adequately  
protected



Estimated  
2021  
cybercrime  
damages:  
\$6 trillion

- Network security makes a growing portion of cyber losses, rising from <5% of incidents in 2017 to ~20% in 2021
  - Attacks originating through phishing account for 4 out of 5 security incidents, with 94% of malware delivered by email
  - Data privacy still makes up over 50% of incidents
- Market concentration increases vulnerability and repeat attacks ([Geer et al, 2020](#))
- Global cyber insurance market size as of 2020 estimated at \$7.8B, with expected 21% CAGR through 2025



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# Current Cyber Insurance Pricing

- Risk factor-based underwriting with focus on industry revenue, employee and record count ([Gallagher, 2021](#))
- Pricing strategies include: ([FTC \(USA\), 2019](#))
  - Flat rate based on frequency-severity for different types of coverage
  - Base rate depending on company revenues
  - Qualitative/survey-based
- Qualitative cyber risk evaluation usually affected by misrepresentations ([UNIVPM, 2019](#))
- Limited data availability among key challenges ([AAA, 2019](#))
- Not understanding cyber exposure → customers see less value in cyber insurance ([Geneva Association, 2018](#))
- The more quantifiable the exposure and loss, the better



# Scope of Presentation

- Spread of risk based on IT network structure
- Broad risks – data access, business interruption
- Binary approach – risk either propagates or does not
  - Not considering partial impacts
  - Not considering specific attack types due to variety and complexity
- Not tackling reputational/legal risk
  - Definitions and ramifications may vary greatly by industry and company





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# Constructing a Model

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# Review of Existing Research

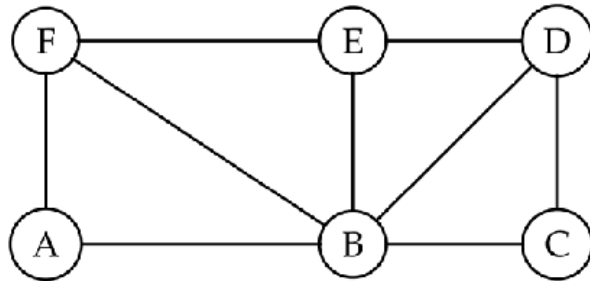
- Network theory has previously been applied in analyses of cyber-physical system vulnerability
  - Zhu, Milanović and Mihić (2019) identified node degree, node importance, betweenness and closeness centrality as key importance measures in vulnerability analysis
  - Zhu and Milanović (2017) used weighted adjacency matrices to analyse system interdependency and vulnerability
  - Guo, Yu et al (2019) constructed a stochastic cyber-physical power system model to investigate cascading failure
  - Fan et al (2020) defined 3 categories of damages: destruction of availability, integrity, and confidentiality of data
- Böhme and Schwartz (2010) presented an early framework on cyber-insurance
  - Five key components: supply side, demand side, info structure, organizational and network environments
  - Defines risk arrival and propagation
- Gil, Kott and Barabási (2014) applied a framework of genetic mutation impact on diseases, to ascertain associations between network services and cyber threats
- Shetty et al (2009) observed that the presence of competitive cyber-insurers may weaken incentives for users to improve their security



# Network Theory – The ABC's

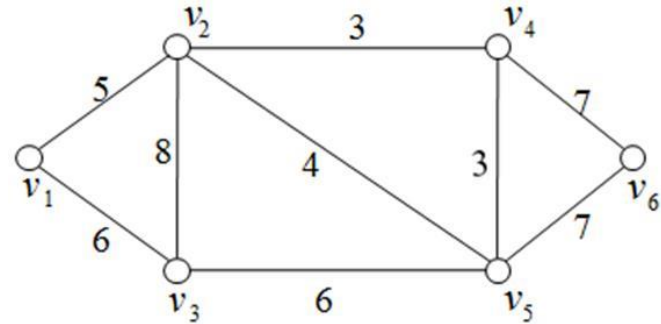
- Study of how objects in a system are related

Unweighted graph



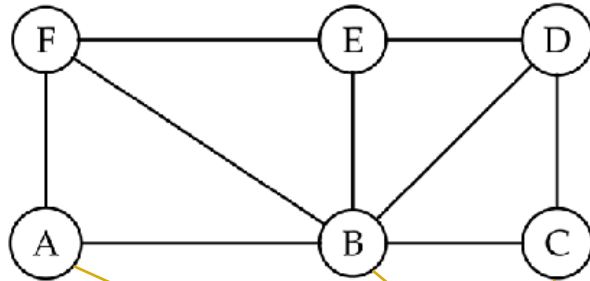
[Source](#)

Weighted graph

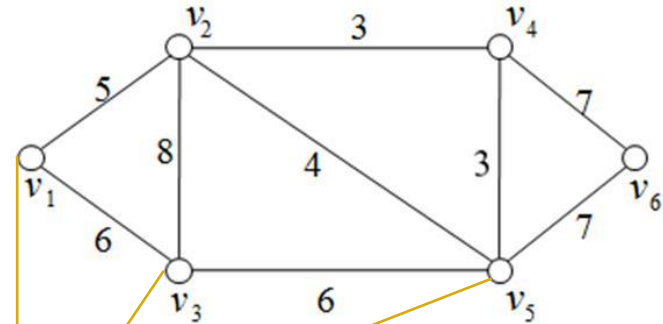


# Network Theory – The ABC's

Unweighted graph



Weighted graph

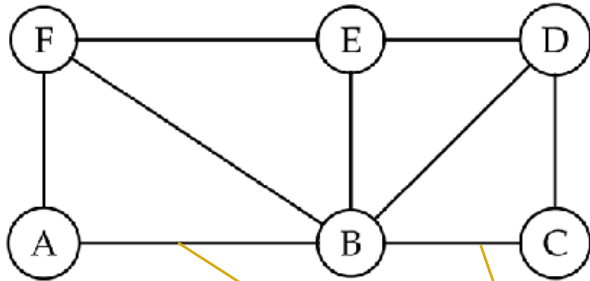


Vertices, or "nodes"

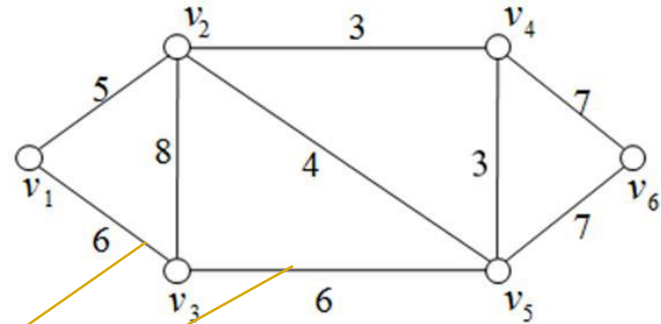


# Network Theory – The ABC's

Unweighted graph



Weighted graph

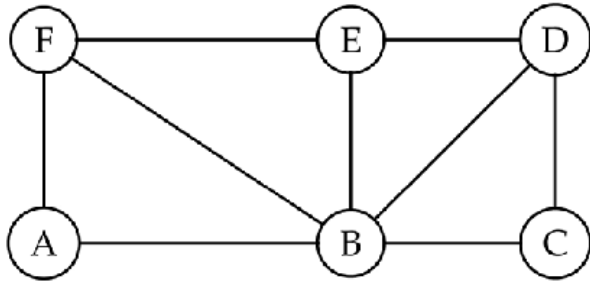


Edges

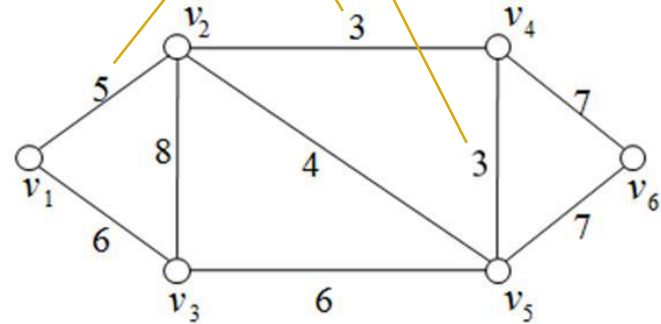


# Network Theory – The ABC's

Unweighted graph



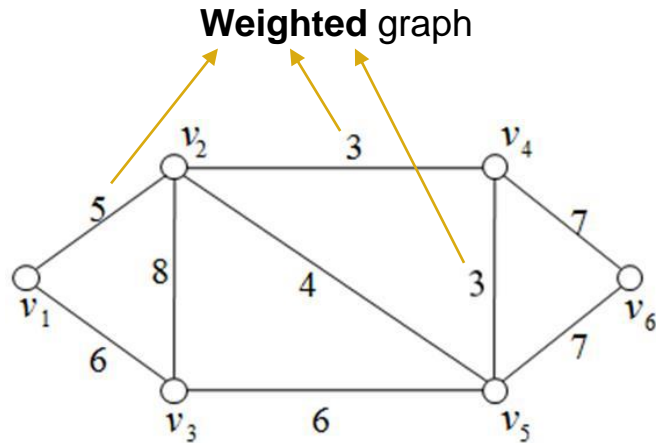
Weighted graph



e.g. traveling salesman problem



# Network Theory – The ABC's



Adjacency matrix

| $v_1$ | $v_2$ | $v_3$ | $v_4$ | $v_5$ | $v_6$ |
|-------|-------|-------|-------|-------|-------|
| 0     | 5     | 6     | 0     | 0     | 0     |
| 5     | 0     | 8     | 3     | 4     | 0     |
| 6     | 8     | 0     | 0     | 6     | 0     |
| 0     | 3     | 0     | 0     | 3     | 7     |
| 0     | 4     | 6     | 3     | 0     | 7     |
| 0     | 0     | 0     | 7     | 7     | 0     |

e.g.  $v_1$  is connected to  $v_2$  with an edge weight of 5, so in the adjacency matrix, we populate elements  $[2^{\text{nd}} \text{ row}, 1^{\text{st}} \text{ column}]$  and  $[1^{\text{st}} \text{ row}, 2^{\text{nd}} \text{ column}]$  with 5

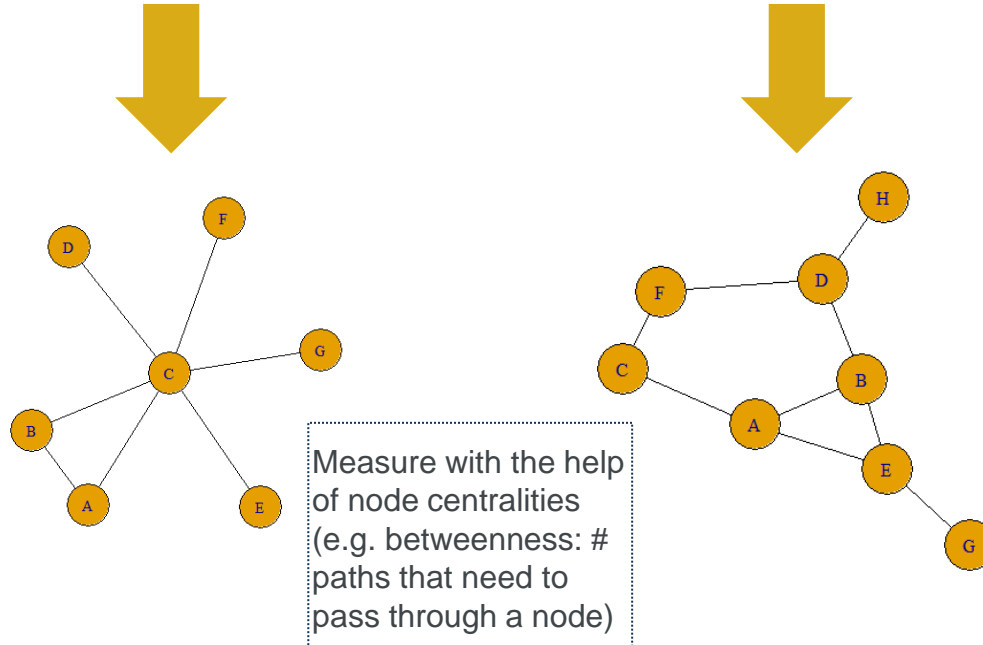


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# Network Theory – The ABC's

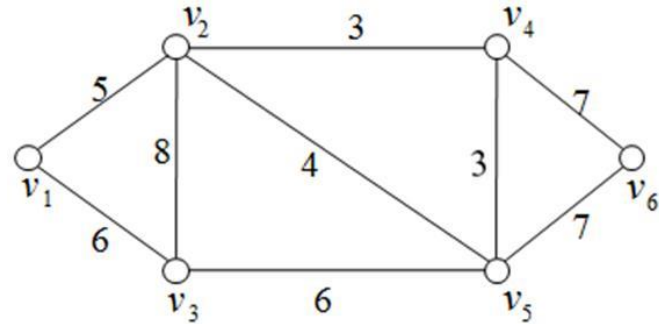
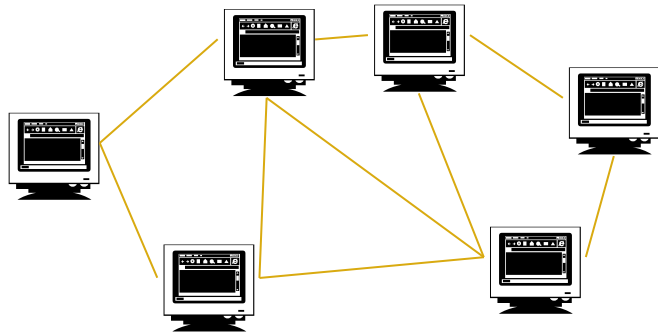
- Concentration of a network

This network is **more concentrated** than this network



# Organization Network Infrastructure

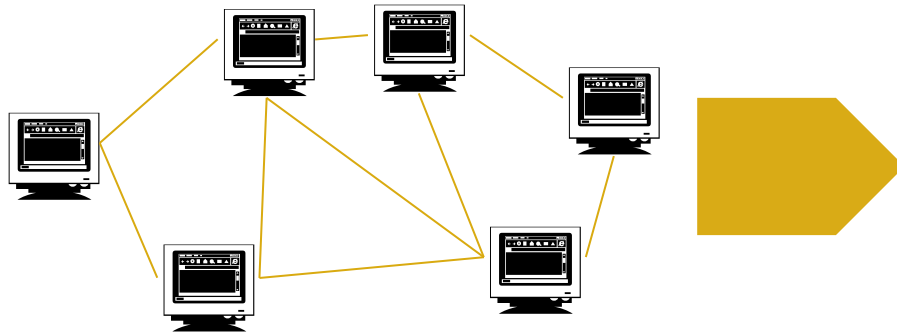
- A set of interconnected workstations
  - Represented through weighted graph
  - Security protocol and strength





# Organization Network Infrastructure

- Basis to understand movement of risk
  - Transition steps
  - Effect of network centrality on severity

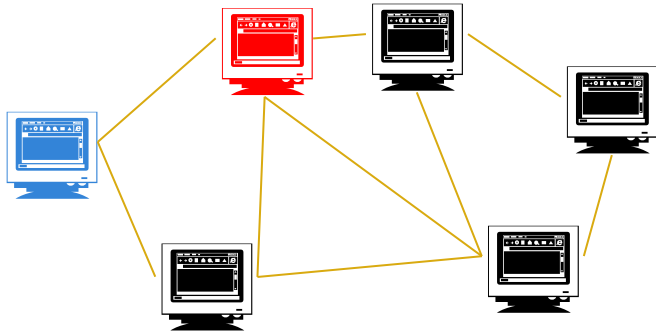


|          |          |          |          |          |          |
|----------|----------|----------|----------|----------|----------|
| 1        | $p_{12}$ | $p_{13}$ | $p_{14}$ | $p_{15}$ | $p_{16}$ |
| $p_{21}$ | 1        | $p_{23}$ | $p_{24}$ | $p_{25}$ | $p_{26}$ |
| $p_{31}$ | $p_{32}$ | 1        | $p_{34}$ | $p_{35}$ | $p_{36}$ |
| $p_{41}$ | $p_{42}$ | $p_{43}$ | 1        | $p_{45}$ | $p_{46}$ |
| $p_{51}$ | $p_{52}$ | $p_{53}$ | $p_{54}$ | 1        | $p_{56}$ |
| $p_{61}$ | $p_{62}$ | $p_{63}$ | $p_{64}$ | $p_{65}$ | 1        |



# Probability Calculation

- Measuring the probability that the attack transfers from node 1 (blue) to node 2 (red) would need to consider the nodes' connectivity
  - Mean-field approximation on very large networks in epidemic models (e.g.  $\epsilon$ -SIS, Pastor-Satorras and Vespignani, n-Intertwined)



$p_{12}$ , or  $P(1 \text{ infects } 2 \mid 1 \text{ is infected})$

=  $P(1 \text{ infects } 2) / P(1 \text{ infects adjacent node})$

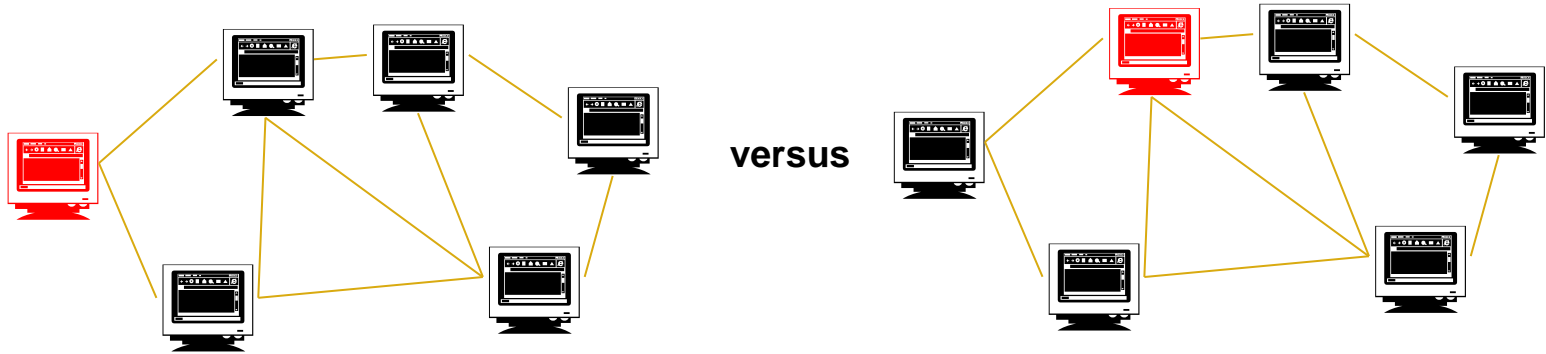
=  $F(\text{Closeness}_{1,2}, \text{Importance}_2) / F(\text{Degree}_1, \text{Importance}_1)$

- Akin to SIS model
  - Still possible to get infected again

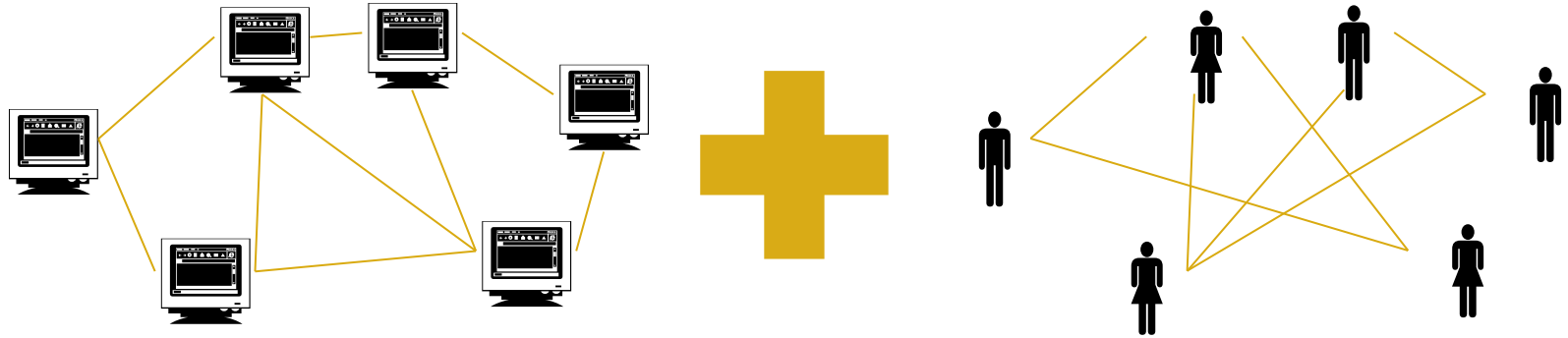


# Determining Spread of Attacks

- Patient zero
  - Internal vs external (how would behaviour change?)
- Path of least resistance?



# Impact of Corporate Social Networks



# Impact of Corporate Social Networks

- Social network analysis
  - Organisational structure
  - Social engineering
  - Privacy concerns
- Internal attacks
  - Modelling behavioural element
- Using a “fire drill” to gauge susceptibility
  - Needs familiarity and expertise, but pros outweigh cons



# Risk Scenarios

- Define objective
  - Motivation in internal attack scenarios
- Select various origins of breach for each scenario
- Consider different network cyberattack strategies
  - Attack sophistication (online presence of company?)
  - How would people respond to the attack?
  - How would the firm as a whole respond? How fast can it respond?
  - Complexity of existing security protocols
- Monitor risk levels using defined metrics
  - Zhu ([2019](#)) defines 2 methods to measure cyberattack success on firewall:
    - Rejected Attempts/Total Traffic
    - Malicious Packets/Total Packets bypassing firewall for a given rule





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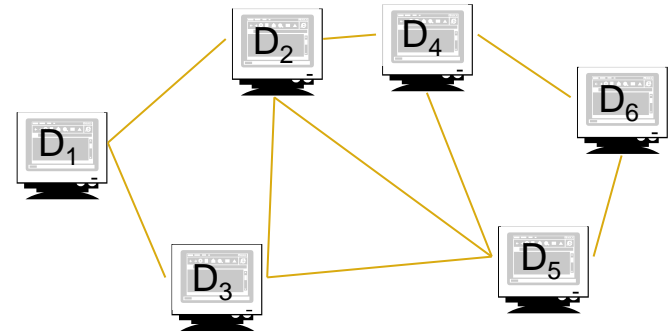
# Using the Model for Pricing

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# Data Vulnerability and Value

- Metric: Total data-at-risk (based on probability of risk transfer,  $p_{ij}$ )
- For a single-step transition, if each workstation  $i$  has volume of data  $D_i$ , then

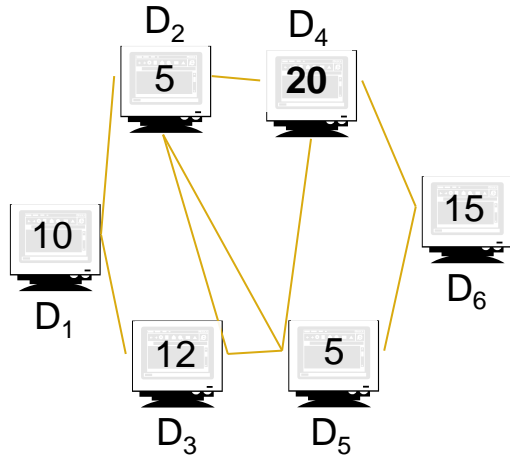
$$\begin{pmatrix} D_1 \\ D_2 \\ D_3 \\ D_4 \\ D_5 \\ D_6 \end{pmatrix}^T \begin{pmatrix} 1 & p_{12} & p_{13} & p_{14} & p_{15} & p_{16} \\ p_{21} & 1 & p_{23} & p_{24} & p_{25} & p_{26} \\ p_{31} & p_{32} & 1 & p_{34} & p_{35} & p_{36} \\ p_{41} & p_{42} & p_{43} & 1 & p_{45} & p_{46} \\ p_{51} & p_{52} & p_{53} & p_{54} & 1 & p_{56} \\ p_{61} & p_{62} & p_{63} & p_{64} & p_{65} & 1 \end{pmatrix} = \begin{pmatrix} \text{DaR}_1 \\ \text{DaR}_2 \\ \text{DaR}_3 \\ \text{DaR}_4 \\ \text{DaR}_5 \\ \text{DaR}_6 \end{pmatrix}$$



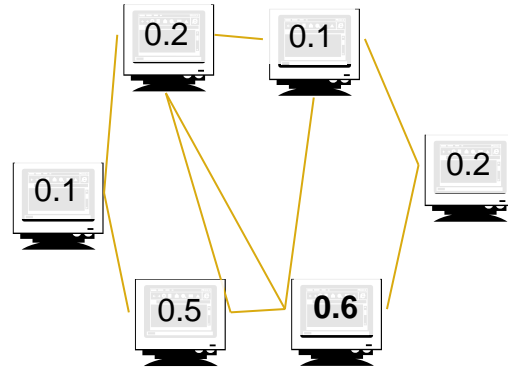
- How does total risk evolve over policy duration?
  - Contingent on centrality of network
- Price based on threshold? Data point?



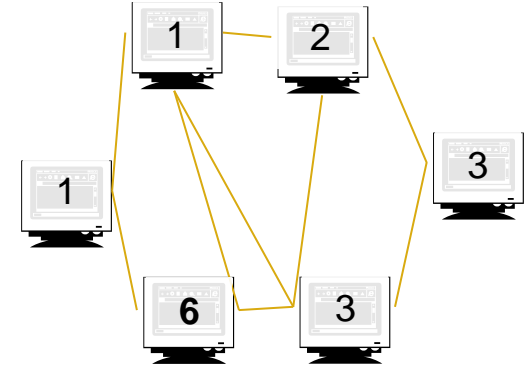
# Data Vulnerability – Example



Data present



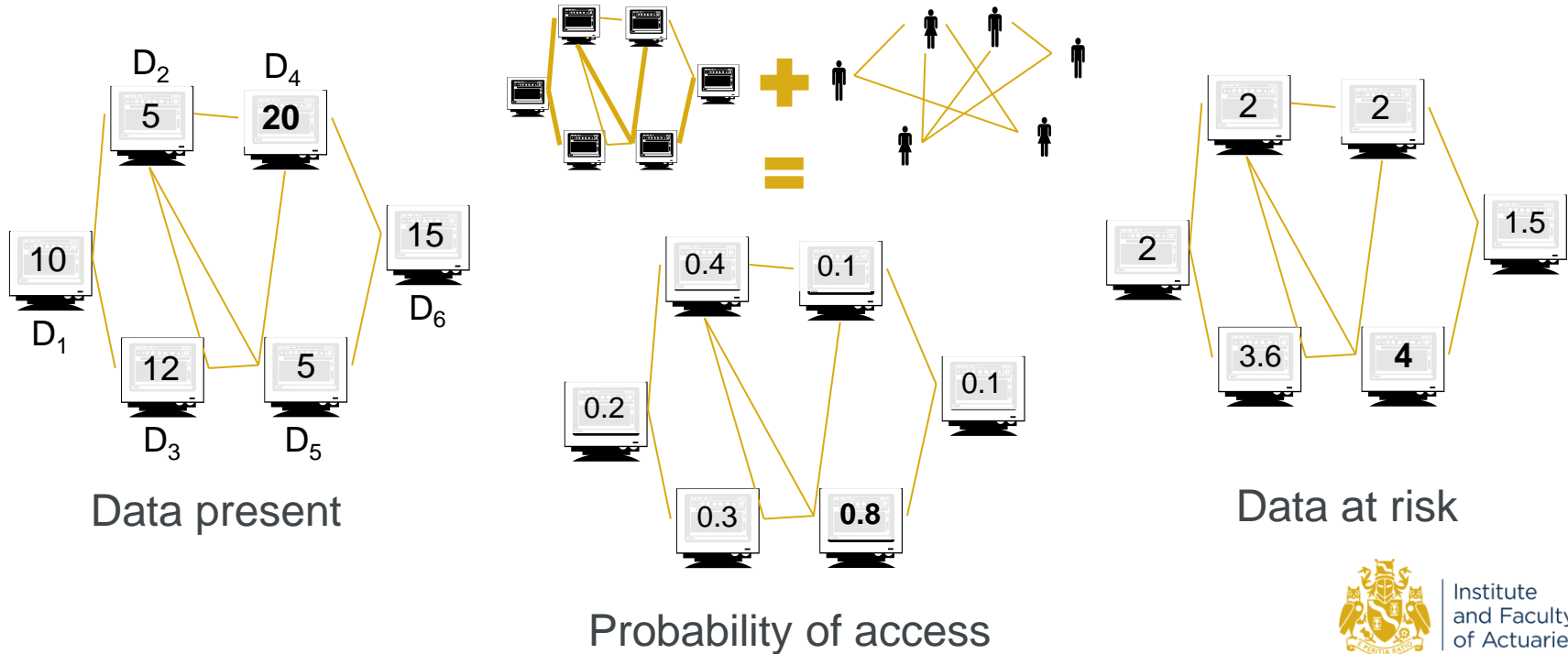
Probability of access



Data at risk



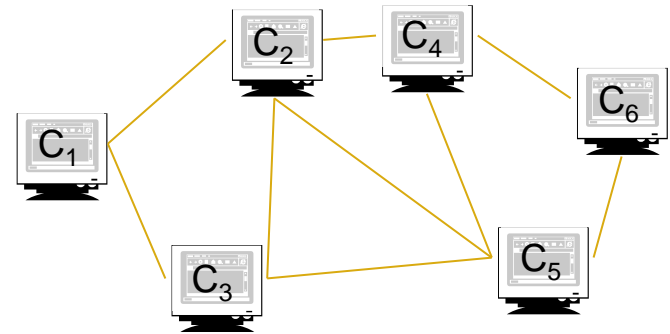
# Data Vulnerability – Example 2



# Business Interruption

- Metric: Expected downtime (capacity below threshold & recoverability)
- Capacity of workstation or center (how fast can each workstation recover?)

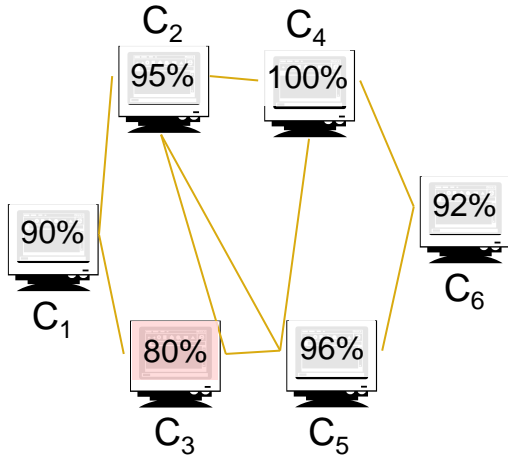
$$\begin{matrix} \mathbf{T} \\ \left( \begin{array}{c} C_1 \\ C_2 \\ C_3 \\ C_4 \\ C_5 \\ C_6 \end{array} \right) \end{matrix} \begin{pmatrix} r_1 & p_{12} & p_{13} & p_{14} & p_{15} & p_{16} \\ p_{21} & r_2 & p_{23} & p_{24} & p_{25} & p_{26} \\ p_{31} & p_{32} & r_3 & p_{34} & p_{35} & p_{36} \\ p_{41} & p_{42} & p_{43} & r_4 & p_{45} & p_{46} \\ p_{51} & p_{52} & p_{53} & p_{54} & r_5 & p_{56} \\ p_{61} & p_{62} & p_{63} & p_{64} & p_{65} & r_6 \end{pmatrix} = \begin{pmatrix} C'_1 \\ C'_2 \\ C'_3 \\ C'_4 \\ C'_5 \\ C'_6 \end{pmatrix}$$



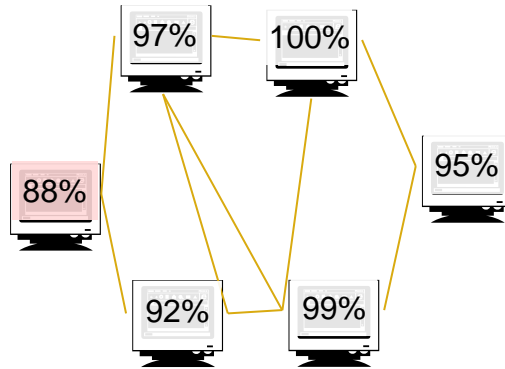
- Set thresholds to determine proper functioning, e.g.  $C > 90\%$
- Number of workstations overloaded  $\rightarrow$  use to determine downtime
  - E.g. DDOS

# Business Interruption - Example

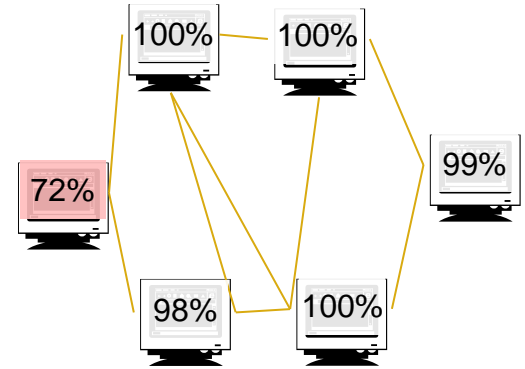
- Threshold of 90%



Network at  $t = 5$



Network at  $t = 6$



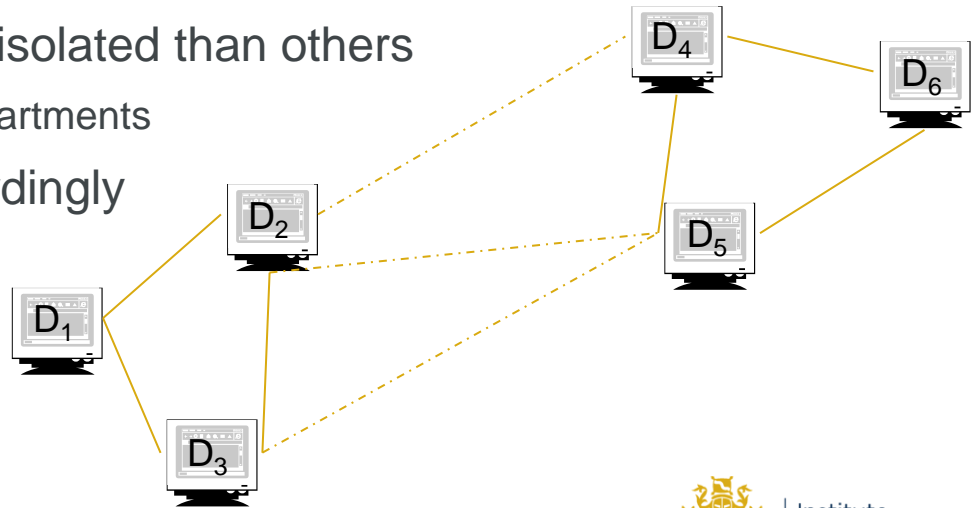
Network at  $t = 7$

- Between  $t = 5$  and  $t = 7$ , station 3 has an expected downtime of 1 while station 1 has an expected downtime of 2



# Insuring Specific Nodes and Sub-Networks

- Certain nodes may be more important, so more targeted
  - E.g. data centres, workstations of members with public exposure
- Some sub-networks may be more isolated than others
  - Geographic dispersion, specific departments
- Need to adjust edge weights accordingly
- Determine risk entry points
  - Origin from obscure network node



# Other Uses

- Cyber risk capital allocation based on attack scenario results
  - Determine VaR/CTE based on worst impacts
- Identification of own weak points
  - Turning descriptive into prescriptive analysis
  - Costs vs benefits of different network architecture ([ASTIN, 2018](#))
  - Addressing silent cyber as a result
  - Antifragility e.g. Chaos Monkey





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# Takeaways and Conclusions

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# Takeaways and Conclusions

- Network theory presents a way to look at cyber risk on a highly granular level
- Subcategories of risks modelled through same framework
  - Data
  - Interruption
- Propagation of risk across a system can be modeled with dynamic scenarios





# Considerations

- Evolution of risk with work-from-home environments
- $A \rightarrow B$  may not be same as  $B \rightarrow A$ 
  - Directed graphs?
  - Workstations with and without certain permissions?
- Moral hazard
- Continuous time modelling
- Blockchain
- Benchmarks for smaller companies (SMEs)
  - Insurability based on size
  - Third-party/IT service usage



# Further Information for Interest

- Literature

- Network attack detection ([MIT, 2019](#))
- Cybersecurity incident prediction through mandatory disclosure regulation ([Berkeley, 2020](#))
- Understanding human decisions in cybersecurity ([Carnegie Mellon, 2014](#))

- Data

- [USB-IDS](#) – Public intrusion detection dataset for more complex analysis of cybersecurity attacks
- [VizSec](#) – Comprehensive list of open-source datasets pertaining to cybersecurity
- [TowerStreet](#) – Data containing 37,500 unique breach incidents
- [Privacy Rights Clearinghouse](#) – Chronology of recent data breaches with details



# Questions

# Comments

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